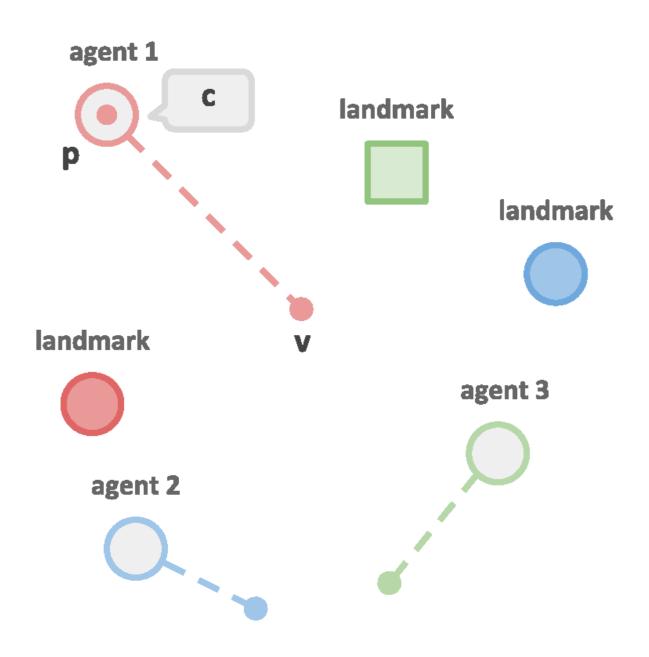
Emergence of Grounded Compositional Language in Multi-Agent Populations

Igor Mordatch, Pieter Abbeel

Environment

- multi-agent reinforcement learning
- cooperative agents
- partially observable state (POMDP), but collectively, state is fully observed
- agents act independently
- takes place in 2d continuous euclidean space
- end-to-end differentiable
- fixed episode length



State

Entities:

- M landmarks
 - position (relative!)
 - color
- N agents
 - $\circ~$ all of the above
 - velocity
 - gaze (pointer)

Other state:

- memory bank (private)
- goals (private)
 - action
 - go to, look at, or do nothing (one hot)
 - target agent
 - location
- utterance (public)
 - one hot encoding in vocab of size K

Actions

- accelerate along some vector
- set new look-at
- softmax over symbols to emit
- update memory banks

Dynamics

position and velocity updated as usual

- γ is a damping factor (friction)
- $f\ {\rm is}\ {\rm used}\ {\rm for}\ {\rm collision}\ {\rm forces},\ {\rm should}\ {\rm be}\ {\rm smooth}$

$$\begin{bmatrix} \mathbf{p} \\ \dot{\mathbf{p}} \\ \mathbf{v} \end{bmatrix}_{i}^{t} = \begin{bmatrix} \mathbf{p} + \dot{\mathbf{p}}\Delta t \\ \gamma \dot{\mathbf{p}} + (\mathbf{u}_{p} + \mathbf{f}(\mathbf{x}_{1}, ..., \mathbf{x}_{N}))\Delta t \\ \mathbf{u}_{v} \end{bmatrix}_{i}^{t-1}$$

- Symbols emitted show up in the environment in the next time step
- Memory banks are updated as well

Reward

$$r_i^t = -\left(\begin{bmatrix} \|\mathbf{p}_r^t - \bar{\mathbf{r}}\|^2 \\ \|\mathbf{v}_r^t - \bar{\mathbf{r}}\|^2 \\ 0 \end{bmatrix}^{\mathsf{T}} \mathbf{g}^{\mathsf{type}} + \|\mathbf{u}_i^t\|^2 + \|\mathbf{c}_i^t\|^2 \right)$$

$$R = r_c + r_g + \sum_t \sum_i r_i^t$$

Training Algorithm

Make sure everything is fully differentiable, and then run backpropagation.

- 1. generate batch-size = 1024 random starting environments
- 2. run dynamics forward and compute total reward
- 3. run backprop and apply gradients

Gumbel-Softmax Estimator

 ϵ is drawn from the Gumbel distribution For a categorical distribution with parameters $p_1, \cdots p_k$, we sample $\epsilon_1, \cdots, \epsilon_k$. Then $\log p_i + \epsilon_i$ will be greater than all other $\log p_j + \epsilon_j$ with probability p_i .

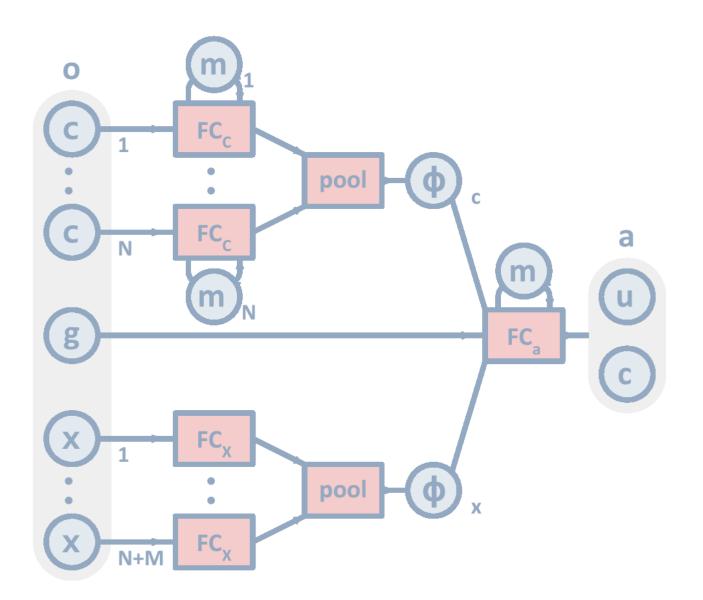
Forward pass:

$$c = ext{sample}(ext{softmax}(\log ec{p} + ec{\epsilon}))$$

Backward pass:

$$rac{dc}{dp} = rac{d}{dp} \mathrm{softmax}(\log ec{p} + ec{\epsilon})$$

Network Architecture



Modules

- allows for training on variable number of landmarks and agents
- each module has independent memory unit
- each module has two layers of 256 units, and a memory size of 32
- input size: ? + 32 (m)
- output size: 256 + 32 (Δm)
- · shared weights across all modules of the same type
- unshared memories

Memory update:

 $\mathbf{m}^{t} = \tanh(\mathbf{m}^{t-1} + \Delta \mathbf{m}^{t-1} + \boldsymbol{\varepsilon})$

Softmax pooling is used to deal with multiple agents/landmarks Gaussian output noise

Prediction Reward

Auxiliary output is prediction of other agent's goals.

$$r_g = -\sum_{\{i,j|i\neq j\}} \|\hat{\mathbf{g}}_{i,j}^T - \mathbf{g}_j^T\|^2$$

MSE even for categorical goal-type and target agent.

Small Vocabulary Reward

Dirichlet process

Suppose n^t words have already been used at time t and the kth word has been used n^t_k times.

$$p_{t+1}(k) = \frac{n_k^t + \alpha K^{-1}}{\alpha + n^t - 1}$$

In order to encourage this, maximize the log-likelihood:

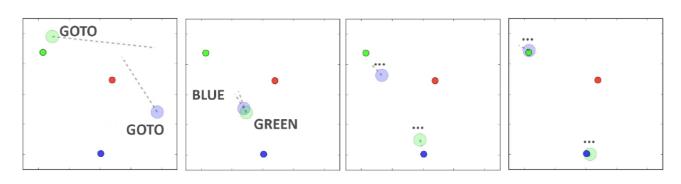
$$r_c = \sum_t \sum_i \log p_t(c_i)$$

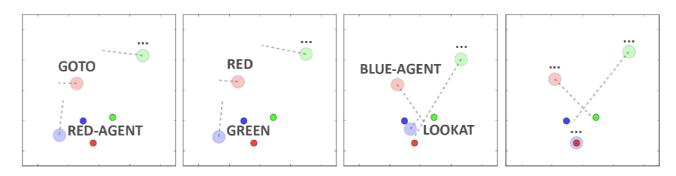
Accumulate counts over:

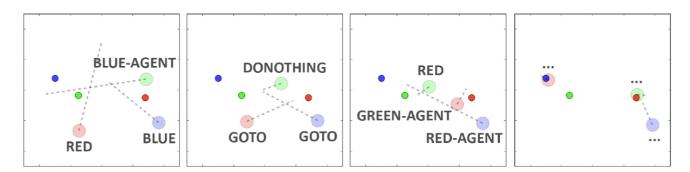
- time steps
- agents

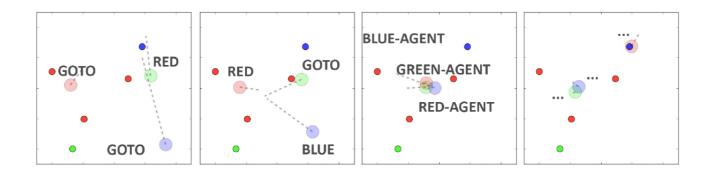
• batches

Results

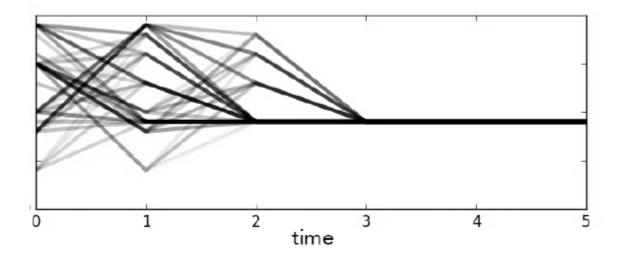






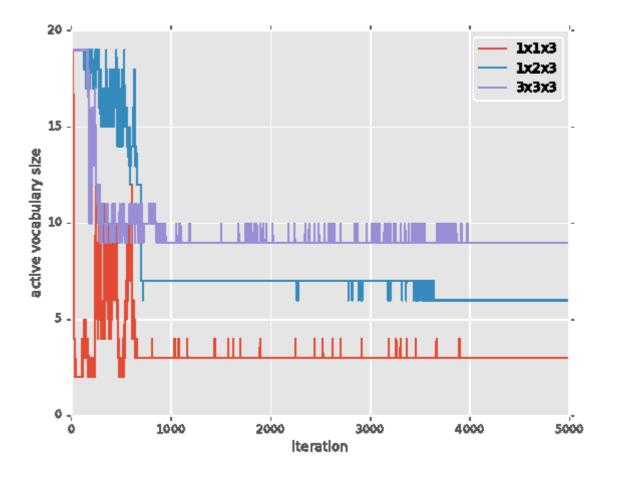


Communication:



More complex requirements require larger language

- 1x1x3: 2 agents, 1 action, 3 landmarks
- 1x2x3: 2 agents, 2 actions, 3 landmarks
- 3x3x3, 4 agents, 3 actions, 3 landmarks



Agents cannot see each other:

Condition	Train Reward	Test Reward
No Communication	-0.919	-0.920
Communication	-0.332	-0.392

Generalization

- Agents will go to the center of two landmarks with the same color if one is referenced.
- If multiple agents have the same color, all will follow instructions from a referring agent.

Nonverbal Communication

- Use of gaze to point to landmarks
- Use of pushing and collision physics to push agents towards landmarks